

# Example: Microsatellite data set

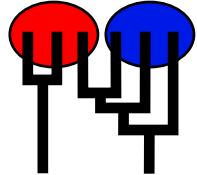
## MIGRATION RATE AND POPULATION SIZE ESTIMATION

using the coalescent and maximum likelihood or Bayesian inference

Migrate-n version 2.5.1

Program started at Thu Jul 10 07:52:44 2008

Program finished at Thu Jul 10 07:53:20 2008



## Options

Datatype:

Microsatellite data [Brownian motion]

Missing data:

not included

Random number seed:

(with internal timer) 1598441029

Start parameters:

Theta values were generated

from the FST-calculation

M values were generated

from the FST-calculation

Connection type matrix:

where m = average (average over a group of Thetas or M,

s = symmetric M, S = symmetric 4Nm, 0 = zero, and not estimated,

\* = free to vary, Thetas are on diagonal

Population 1 2

1 population\_num \* \*

2 population\_num \* \*

Order of parameters:

|   |                       |             |
|---|-----------------------|-------------|
| 1 | $\Theta_1$            | <displayed> |
| 2 | $\Theta_2$            | <displayed> |
| 3 | $M_{2 \rightarrow 1}$ | <displayed> |
| 4 | $M_{1 \rightarrow 2}$ | <displayed> |

Mutation rate among loci:

Mutation rate is constant for all loci

Analysis strategy:

Bayesian inference

Proposal distributions for parameter

Parameter Proposal

|   |                            |          |           |             |       |      |  |  |
|---|----------------------------|----------|-----------|-------------|-------|------|--|--|
| Theta   | Slice sampling             |          |           |             |       |      |  |  |
| M   | Slice sampling             |          |           |             |       |      |  |  |
| Prior distribution for parameter                  |                            |          |           |             |       |      |  |  |
| Parameter   | Prior                      | Minimum  | Mean*     | Maximum     | Delta | Bins |  |  |
| Theta   | Exponential                | 0.000000 | 1.000000  | 10.000000   | -     | 200  |  |  |
| M   | Exponential                | 0.000000 | 10.000000 | 1000.000000 | -     | 200  |  |  |
| Markov chain settings:                            |                            |          |           |             |       |      |  |  |
| Number of chains                                  | Long chain                 |          |           |             |       |      |  |  |
| Recorded steps [a]                                | 1                          |          |           |             |       |      |  |  |
| Increment (record every x step [b])               | 1600                       |          |           |             |       |      |  |  |
| Number of concurrent chains (replicates) [c]      | 2                          |          |           |             |       |      |  |  |
| Visited (sampled) parameter values [a*b*c]        | 2                          |          |           |             |       |      |  |  |
| Number of discard trees per chain (burn-in)       | 6400                       |          |           |             |       |      |  |  |
| Multiple Markov chains:                           | 130                        |          |           |             |       |      |  |  |
| Static heating scheme                             | 4 chains with temperatures |          |           |             |       |      |  |  |
|   | 5.00                       | 3.67     | 2.33      | 1.00        |       |      |  |  |
|   | Swapping interval is 1     |          |           |             |       |      |  |  |
| Print options:                                    |                            |          |           |             |       |      |  |  |
| Data file:  | infile.msat                |          |           |             |       |      |  |  |
| Output file:                                      | outfile-bayes              |          |           |             |       |      |  |  |
| Posterior distribution raw histogram file:        | bayesfile                  |          |           |             |       |      |  |  |
| Print data:                                       | No                         |          |           |             |       |      |  |  |
| Print genealogies [only some for some data type]: | None                       |          |           |             |       |      |  |  |

## Data summary

| Datatype:                | Microsatellite data |                               |
|--------------------------|---------------------|-------------------------------|
| Number of loci:          | 10                  |                               |
| Population               | Locus               | Gene copies<br>data (missing) |
| 1 population_number_0    | 1                   | 50 (0)                        |
|                          | 2                   | 50 (0)                        |
|                          | 3                   | 50 (0)                        |
|                          | 4                   | 50 (0)                        |
|                          | 5                   | 50 (0)                        |
|                          | 6                   | 50 (0)                        |
|                          | 7                   | 50 (0)                        |
|                          | 8                   | 50 (0)                        |
|                          | 9                   | 50 (0)                        |
|                          | 10                  | 50 (0)                        |
| 2 population_number_1    | 1                   | 42 (0)                        |
|                          | 2                   | 42 (0)                        |
|                          | 3                   | 42 (0)                        |
|                          | 4                   | 42 (0)                        |
|                          | 5                   | 42 (0)                        |
|                          | 6                   | 42 (0)                        |
|                          | 7                   | 42 (0)                        |
|                          | 8                   | 42 (0)                        |
|                          | 9                   | 42 (0)                        |
|                          | 10                  | 42 (0)                        |
| Total of all populations | 1                   | 92 (0)                        |
|                          | 2                   | 92 (0)                        |
|                          | 3                   | 92 (0)                        |
|                          | 4                   | 92 (0)                        |
|                          | 5                   | 92 (0)                        |
|                          | 6                   | 92 (0)                        |
|                          | 7                   | 92 (0)                        |
|                          | 8                   | 92 (0)                        |
|                          | 9                   | 92 (0)                        |
|                          | 10                  | 92 (0)                        |

## *Allele frequency spectra*

Locus 1

| Allele | Pop1 | Pop2 | All |
|--------|------|------|-----|
|--------|------|------|-----|

|    |       |       |       |
|----|-------|-------|-------|
| 16 | 0.220 | 0.167 | 0.193 |
| 19 | 0.040 | 0.071 | 0.056 |
| 18 | 0.060 | 0.119 | 0.090 |
| 15 | 0.220 | 0.024 | 0.122 |
| 21 | 0.020 | 0.167 | 0.093 |
| 23 | 0.020 | 0.119 | 0.070 |
| 17 | 0.280 | 0.095 | 0.188 |
| 22 | 0.060 | 0.119 | 0.090 |
| 25 | 0.060 | 0.024 | 0.042 |
| 24 | 0.020 | 0.000 | 0.010 |
| 26 | 0.000 | 0.024 | 0.012 |
| 27 | 0.000 | 0.048 | 0.024 |
| 29 | 0.000 | 0.024 | 0.012 |

Locus 2

| Allele | Pop1 | Pop2 | All |
|--------|------|------|-----|
|--------|------|------|-----|

|    |       |       |       |
|----|-------|-------|-------|
| 16 | 0.520 | 0.571 | 0.546 |
| 19 | 0.040 | 0.000 | 0.020 |
| 18 | 0.220 | 0.119 | 0.170 |
| 17 | 0.160 | 0.167 | 0.163 |
| 15 | 0.020 | 0.000 | 0.010 |
| 21 | 0.020 | 0.071 | 0.046 |
| 20 | 0.020 | 0.024 | 0.022 |
| 22 | 0.000 | 0.048 | 0.024 |

Locus 3

| Allele | Pop1 | Pop2 | All |
|--------|------|------|-----|
|--------|------|------|-----|

|    |       |       |       |
|----|-------|-------|-------|
| 19 | 0.240 | 0.262 | 0.251 |
| 20 | 0.280 | 0.476 | 0.378 |
| 18 | 0.080 | 0.095 | 0.088 |
| 21 | 0.280 | 0.119 | 0.200 |
| 22 | 0.120 | 0.048 | 0.084 |

Locus 4

| Allele | Pop1 | Pop2 | All |
|--------|------|------|-----|
|--------|------|------|-----|

|    |       |       |       |
|----|-------|-------|-------|
| 16 | 0.080 | 0.071 | 0.076 |
| 24 | 0.180 | 0.024 | 0.102 |

| Allele         | Pop1  | Pop2  | All   |
|----------------|-------|-------|-------|
| 15             | 0.020 | 0.048 | 0.034 |
| 25             | 0.160 | 0.167 | 0.163 |
| 14             | 0.020 | 0.048 | 0.034 |
| 19             | 0.100 | 0.143 | 0.121 |
| 12             | 0.060 | 0.000 | 0.030 |
| 20             | 0.080 | 0.190 | 0.135 |
| 23             | 0.060 | 0.119 | 0.090 |
| 28             | 0.020 | 0.000 | 0.010 |
| 22             | 0.060 | 0.024 | 0.042 |
| 21             | 0.160 | 0.119 | 0.140 |
| 13             | 0.000 | 0.024 | 0.012 |
| 26             | 0.000 | 0.024 | 0.012 |
| <b>Locus 5</b> |       |       |       |
| Allele         | Pop1  | Pop2  | All   |
| 20             | 0.400 | 0.524 | 0.462 |
| 21             | 0.420 | 0.357 | 0.389 |
| 19             | 0.180 | 0.119 | 0.150 |
| <b>Locus 6</b> |       |       |       |
| Allele         | Pop1  | Pop2  | All   |
| 19             | 0.060 | 0.000 | 0.030 |
| 20             | 0.100 | 0.024 | 0.062 |
| 18             | 0.300 | 0.214 | 0.257 |
| 22             | 0.200 | 0.119 | 0.160 |
| 21             | 0.120 | 0.476 | 0.298 |
| 16             | 0.060 | 0.000 | 0.030 |
| 24             | 0.160 | 0.048 | 0.104 |
| 17             | 0.000 | 0.119 | 0.060 |
| <b>Locus 7</b> |       |       |       |
| Allele         | Pop1  | Pop2  | All   |
| 23             | 0.040 | 0.238 | 0.139 |
| 20             | 0.660 | 0.143 | 0.401 |
| 22             | 0.180 | 0.190 | 0.185 |
| 21             | 0.100 | 0.333 | 0.217 |
| 19             | 0.020 | 0.095 | 0.058 |
| <b>Locus 8</b> |       |       |       |
| Allele         | Pop1  | Pop2  | All   |
| 19             | 0.520 | 0.524 | 0.522 |
| 17             | 0.040 | 0.048 | 0.044 |

| Allele | Pop1 | Pop2 | All |
|--------|------|------|-----|
|--------|------|------|-----|

|    |       |       |       |
|----|-------|-------|-------|
| 18 | 0.100 | 0.071 | 0.086 |
| 20 | 0.140 | 0.190 | 0.165 |
| 16 | 0.080 | 0.000 | 0.040 |
| 22 | 0.100 | 0.048 | 0.074 |
| 15 | 0.020 | 0.048 | 0.034 |
| 23 | 0.000 | 0.071 | 0.036 |

Locus 9

| Allele | Pop1 | Pop2 | All |
|--------|------|------|-----|
|--------|------|------|-----|

|    |       |       |       |
|----|-------|-------|-------|
| 24 | 0.080 | 0.024 | 0.052 |
| 19 | 0.300 | 0.429 | 0.364 |
| 20 | 0.300 | 0.167 | 0.233 |
| 23 | 0.180 | 0.143 | 0.161 |
| 22 | 0.080 | 0.024 | 0.052 |
| 18 | 0.020 | 0.071 | 0.046 |
| 21 | 0.040 | 0.095 | 0.068 |
| 25 | 0.000 | 0.048 | 0.024 |

Locus 10

| Allele | Pop1 | Pop2 | All |
|--------|------|------|-----|
|--------|------|------|-----|

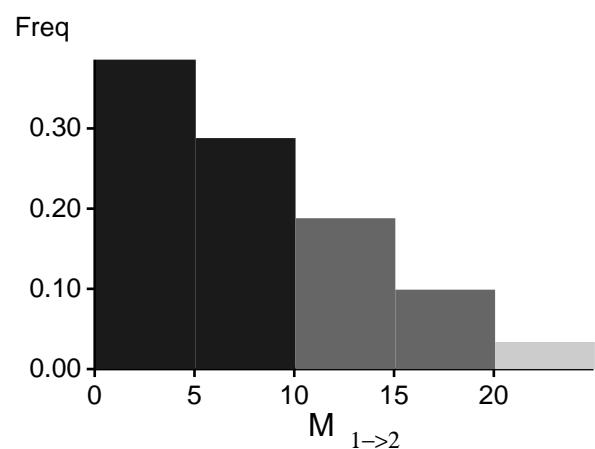
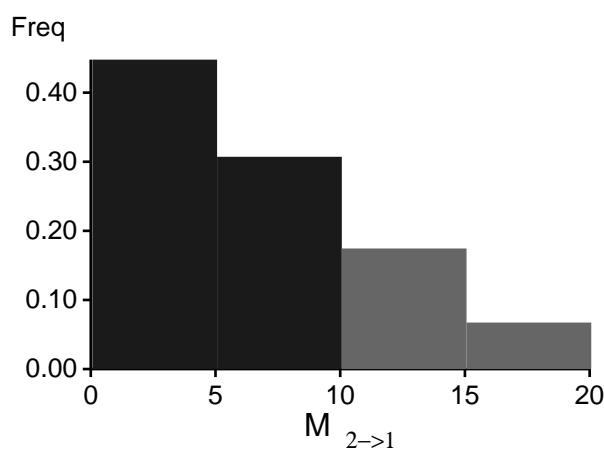
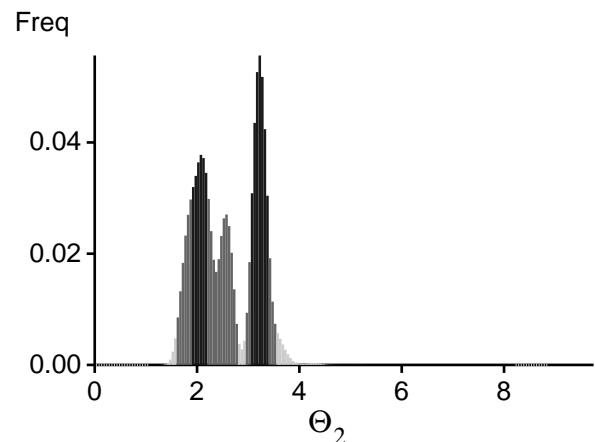
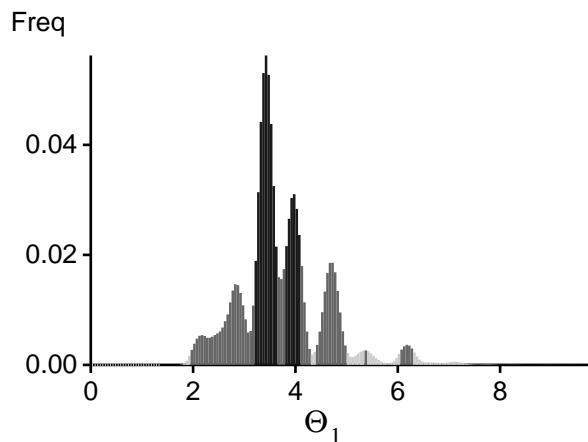
|    |       |       |       |
|----|-------|-------|-------|
| 22 | 0.100 | 0.214 | 0.157 |
| 20 | 0.440 | 0.214 | 0.327 |
| 23 | 0.080 | 0.167 | 0.123 |
| 24 | 0.020 | 0.000 | 0.010 |
| 19 | 0.160 | 0.167 | 0.163 |
| 21 | 0.060 | 0.048 | 0.054 |
| 18 | 0.080 | 0.000 | 0.040 |
| 15 | 0.020 | 0.071 | 0.046 |
| 17 | 0.040 | 0.048 | 0.044 |
| 25 | 0.000 | 0.071 | 0.036 |

## Bayesian Analysis: Posterior distribution table

| Locus | Parameter             | 2.5%    | 25.0%   | Mode    | 75.0%    | 97.5%    | Median  | Mean    |
|-------|-----------------------|---------|---------|---------|----------|----------|---------|---------|
| 1     | $\Theta_1$            | 1.40000 | 3.35000 | 4.32500 | 4.80000  | 5.05000  | 4.52500 | 5.26478 |
|       | $\Theta_2$            | 7.20000 | 8.20000 | 9.77500 | 10.00000 | 10.00000 | 8.27500 | 7.04778 |
|       | $M_{2 \rightarrow 1}$ | 0.000   | 0.000   | 2.500   | 10.000   | 20.000   | 12.500  | 4.223   |
|       | $M_{1 \rightarrow 2}$ | 0.000   | 0.000   | 7.500   | 15.000   | 25.000   | 17.500  | 8.524   |
| 2     | $\Theta_1$            | 1.45000 | 2.80000 | 3.42500 | 4.25000  | 5.80000  | 3.57500 | 3.64177 |
|       | $\Theta_2$            | 1.35000 | 4.50000 | 4.87500 | 5.05000  | 5.60000  | 4.32500 | 5.14776 |
|       | $M_{2 \rightarrow 1}$ | 0.000   | 0.000   | 2.500   | 10.000   | 20.000   | 12.500  | 4.927   |
|       | $M_{1 \rightarrow 2}$ | 0.000   | 0.000   | 2.500   | 15.000   | 25.000   | 17.500  | 7.918   |
| 3     | $\Theta_1$            | 4.35000 | 4.45000 | 4.62500 | 5.35000  | 6.65000  | 5.17500 | 5.46904 |
|       | $\Theta_2$            | 1.15000 | 2.30000 | 2.62500 | 3.30000  | 4.15000  | 2.82500 | 2.78699 |
|       | $M_{2 \rightarrow 1}$ | 0.000   | 0.000   | 2.500   | 10.000   | 20.000   | 12.500  | 4.114   |
|       | $M_{1 \rightarrow 2}$ | 0.000   | 0.000   | 2.500   | 10.000   | 25.000   | 12.500  | 7.319   |
| 4     | $\Theta_1$            | 7.40000 | 8.45000 | 9.82500 | 10.00000 | 10.00000 | 8.57500 | 7.16454 |
|       | $\Theta_2$            | 4.55000 | 8.85000 | 9.07500 | 9.50000  | 10.00000 | 6.47500 | 6.14968 |
|       | $M_{2 \rightarrow 1}$ | 0.000   | 0.000   | 2.500   | 10.000   | 20.000   | 12.500  | 4.626   |
|       | $M_{1 \rightarrow 2}$ | 0.000   | 0.000   | 2.500   | 10.000   | 25.000   | 12.500  | 7.299   |
| 5     | $\Theta_1$            | 1.20000 | 1.45000 | 1.67500 | 3.25000  | 3.65000  | 3.17500 | 4.31662 |
|       | $\Theta_2$            | 1.00000 | 2.80000 | 3.17500 | 3.45000  | 4.70000  | 3.02500 | 3.22268 |
|       | $M_{2 \rightarrow 1}$ | 0.000   | 0.000   | 2.500   | 10.000   | 25.000   | 12.500  | 5.894   |
|       | $M_{1 \rightarrow 2}$ | 0.000   | 0.000   | 2.500   | 10.000   | 25.000   | 12.500  | 6.565   |
| 6     | $\Theta_1$            | 1.75000 | 3.70000 | 4.72500 | 5.25000  | 7.50000  | 4.77500 | 4.73794 |
|       | $\Theta_2$            | 1.30000 | 1.55000 | 1.97500 | 3.50000  | 5.45000  | 4.22500 | 5.06340 |
|       | $M_{2 \rightarrow 1}$ | 0.000   | 0.000   | 2.500   | 10.000   | 25.000   | 12.500  | 5.596   |
|       | $M_{1 \rightarrow 2}$ | 0.000   | 0.000   | 2.500   | 10.000   | 25.000   | 12.500  | 5.391   |
| 7     | $\Theta_1$            | 2.70000 | 4.90000 | 5.27500 | 5.60000  | 7.95000  | 5.37500 | 5.26686 |
|       | $\Theta_2$            | 0.90000 | 1.95000 | 2.57500 | 3.75000  | 7.30000  | 3.92500 | 4.12347 |
|       | $M_{2 \rightarrow 1}$ | 0.000   | 0.000   | 2.500   | 10.000   | 20.000   | 12.500  | 3.821   |
|       | $M_{1 \rightarrow 2}$ | 0.000   | 0.000   | 2.500   | 10.000   | 25.000   | 12.500  | 6.167   |
| 8     | $\Theta_1$            | 3.25000 | 4.40000 | 5.22500 | 6.30000  | 6.40000  | 5.87500 | 6.04024 |
|       | $\Theta_2$            | 0.95000 | 3.50000 | 4.52500 | 5.40000  | 6.95000  | 4.37500 | 4.28143 |
|       | $M_{2 \rightarrow 1}$ | 0.000   | 0.000   | 2.500   | 10.000   | 20.000   | 12.500  | 3.651   |
|       | $M_{1 \rightarrow 2}$ | 0.000   | 0.000   | 2.500   | 15.000   | 25.000   | 17.500  | 6.847   |

## Example: Microsatellite data set -- 8

|     |                       |         |         |         |          |          |         |         |
|-----|-----------------------|---------|---------|---------|----------|----------|---------|---------|
| 9   | $\Theta_1$            | 4.25000 | 6.75000 | 7.37500 | 7.95000  | 8.95000  | 6.12500 | 5.79059 |
| 9   | $\Theta_2$            | 1.05000 | 2.90000 | 3.87500 | 4.50000  | 7.30000  | 3.97500 | 4.40128 |
| 9   | $M_{2 \rightarrow 1}$ | 0.000   | 0.000   | 2.500   | 10.000   | 20.000   | 12.500  | 3.734   |
| 9   | $M_{1 \rightarrow 2}$ | 0.000   | 0.000   | 2.500   | 15.000   | 25.000   | 17.500  | 7.946   |
| 10  | $\Theta_1$            | 7.75000 | 8.35000 | 9.12500 | 10.00000 | 10.00000 | 7.02500 | 6.62277 |
| 10  | $\Theta_2$            | 7.00000 | 8.50000 | 9.67500 | 10.00000 | 10.00000 | 8.17500 | 6.96102 |
| 10  | $M_{2 \rightarrow 1}$ | 0.000   | 0.000   | 2.500   | 10.000   | 20.000   | 12.500  | 4.413   |
| 10  | $M_{1 \rightarrow 2}$ | 0.000   | 0.000   | 7.500   | 15.000   | 30.000   | 17.500  | 10.138  |
| All | $\Theta_1$            | 1.90000 | 3.15000 | 3.42500 | 3.65000  | 4.30000  | 3.62500 | 3.73939 |
| All | $\Theta_2$            | 2.90000 | 3.00000 | 3.22500 | 3.40000  | 3.55000  | 2.62500 | 2.61171 |
| All | $M_{2 \rightarrow 1}$ | 0.000   | 0.000   | 2.500   | 10.000   | 20.000   | 12.500  | 2.752   |
| All | $M_{1 \rightarrow 2}$ | 0.000   | 0.000   | 2.500   | 10.000   | 20.000   | 12.500  | 4.842   |

*Bayesian Analysis: Posterior distribution over all loci*

## *Log-Probability of the data given the model (marginal likelihood)*

Use this value for Bayes factor calculations:

$BF = \text{Exp}[\ln(\text{Prob}(D | \text{thisModel}) - \ln(\text{Prob}(D | \text{otherModel}))$   
shows the support for thisModel]

| Method                    | $\ln(\text{Prob}(D   \text{Model}))$ | Notes |
|---------------------------|--------------------------------------|-------|
| Thermodynamic integration | -11105.469570                        | (1)   |
| Harmonic mean             | -171797.952118                       | (1)   |

(1 and 2) is an approximation to the marginal likelihood, make sure the program run long enough!

(1) and (2) should give a similar result, (2) is considered more  
crude than (1), but (1) needs heating with several well-spaced chains,

*Acceptance ratios for all parameters and the genealogies*

| Parameter             | Accepted changes | Ratio   |
|-----------------------|------------------|---------|
| $\Theta_1$            | 8245/8245        | 1.00000 |
| $\Theta_2$            | 8202/8202        | 1.00000 |
| $M_{2 \rightarrow 1}$ | 8219/8219        | 1.00000 |
| $M_{1 \rightarrow 2}$ | 8362/8362        | 1.00000 |
| Genealogies           | 11457/32296      | 0.35475 |

## MCMC-Autocorrelation and Effective MCMC Sample Size

| Parameter             | Autocorrelation | Effective Sample Size |
|-----------------------|-----------------|-----------------------|
| $\Theta_1$            | 0.96005         | 656.75                |
| $\Theta_2$            | 0.94780         | 865.53                |
| $M_{2 \rightarrow 1}$ | 0.90610         | 1583.93               |
| $M_{1 \rightarrow 2}$ | 0.90364         | 1653.89               |
| Ln[Prob(D G)]         | 0.98468         | 249.13                |